

10/02-10/04 **Objectives**

- Review Homework Questions
- Section 10.1 Rational Expressions, Functions, and Models
- Section 10.2 Rational Numbers as Exponents
- Section 10.3 Multiplying Radical Expressions
- Section 10.4 Dividing Radical Expressions
- Homework:
 - Concept Review
 - Pg. 705 # 1-8
 - Pg. 714 # 1-8
 - Pg. 721 # 1-6
 - Pg. 728 # 1-8
 - Mixed Review
 - Pg. 738 # 1-13

Pg 687 #17

$$M + W + C = 56.7$$

$$W = 3.9 + M$$

$$C = 43.3 + (M + W)$$

Radical Expressions

$$\sqrt{25} = 5$$

$$-\sqrt{64} = -8$$

$$\sqrt{-64} = \text{no solution}$$

$$\sqrt{36x^2} = |6x|$$

$$x = -3$$

$$\sqrt{36(-3)^2} \quad 6(-3)$$

$$\sqrt{324} \quad |-18|$$

$$18 = 18$$

$$\sqrt{(x-1)^2} = |x-1|$$

$$\sqrt{x^2 - 8x + 16} = |x-4|$$

$(x-4)(x-4)$
 $(x-4)^2$

$$\sqrt{x^2 - 4x - 5} \leftarrow \text{Answer}$$

$(x+1)(x-5)$

$$\sqrt{x^2 + 9} \leftarrow \text{Cant simplify}$$

~~$x+3$~~

$$\sqrt[3]{-8x^3} = -2x$$

$$\sqrt[5]{32} = 2$$



$$\sqrt[9]{(x+5)^9} = x+5$$

Old Rules you should know

$$1) x^a \cdot x^b = x^{a+b}$$

$$2) x^a / x^b = x^{a-b}$$

$$3) (x^m)^n = x^{mn}$$

$$4) (xy)^m = x^m y^m$$

$$5) x^0 = 1$$

$$6) x^{-m} = \frac{1}{x^m}$$

Rule 1 of the night

$$a^{m/n} = \sqrt[n]{a^m}$$

$$8^{1/3} = \sqrt[3]{8}$$

$$(25x^{16})^{1/2} = \sqrt{25x^{16}} = 5x^8$$

$$25^{1/2} x^8$$



$$\sqrt[5]{7ab} = (7ab)^{1/5}$$

$$\sqrt[7]{\frac{x^3y}{4}} = \left(\frac{x^3y}{4}\right)^{1/7}$$

$$\sqrt{(5x)^3} = (5x)^{3/2}$$

$$3^{1/5} \cdot 3^{3/5} = 3^{4/5}$$

$$\sqrt[5]{3} \cdot \sqrt[5]{3^3} = \sqrt[5]{3^4}$$

$$\left(\sqrt[3]{ab^2c}\right)^{12} = \left((ab^2c)^{1/3}\right)^{12}$$
$$= (ab^2c)^4$$

$$\sqrt{\sqrt[3]{x}} = \sqrt{(x)^{1/3}} \quad \left(x^{1/3}\right)^{1/2} = x^{1/6}$$

$$\sqrt[3]{\sqrt[4]{xy}} = \sqrt[3]{(xy)^{1/4}} = \left((xy)^{1/4}\right)^{1/3}$$
$$(xy)^{1/12}$$

Multiplication

$$\sqrt{100} = 10$$

$$\sqrt{4} = 2$$

$$\sqrt{25} = 5$$

$$\frac{\sqrt{4} \cdot \sqrt{25}}{\sqrt{100}} = 10$$

$$\sqrt{4 \cdot 25} = 10$$

Rule #2

$$\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{a \cdot b}$$

$$\sqrt{3} \cdot \sqrt{5} = \sqrt{15}$$

$$\begin{aligned}\sqrt{x+3} \cdot \sqrt{x-3} &= \sqrt{(x+3)(x-3)} \\ &= \sqrt{x^2-9}\end{aligned}$$

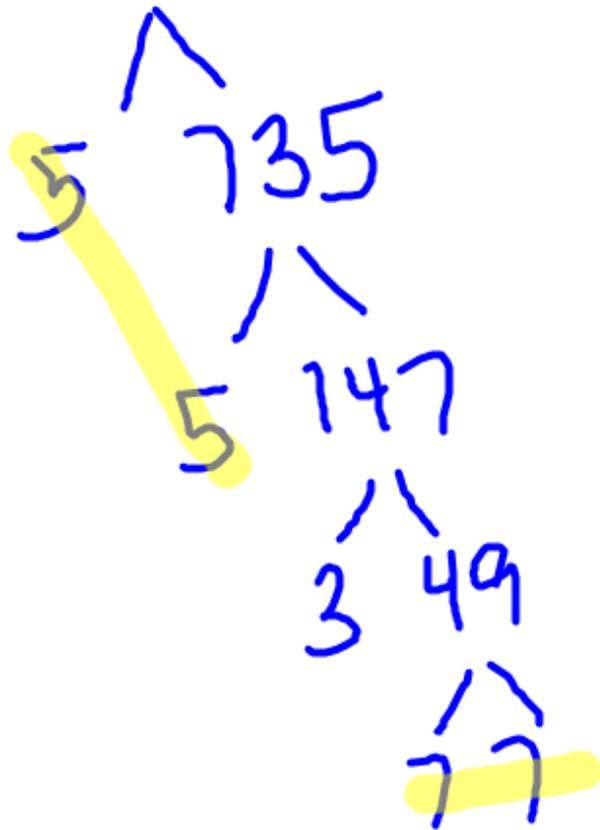
$$\sqrt{200} = \sqrt{100 \cdot 2} = \sqrt{100} \cdot \sqrt{2} = 10\sqrt{2}$$



$$= 2 \cdot 5 \sqrt{2}$$



$$\sqrt{3675} = 5 \cdot 7 \sqrt{3}$$



$$35\sqrt{3}$$

$$\sqrt{18x^2y} = \sqrt{18} \sqrt{x^2} \sqrt{y}$$

$\begin{array}{c} \swarrow \searrow \\ 9 \quad 2 \\ \swarrow \searrow \\ 3 \quad 3 \end{array}$ \downarrow \downarrow
 x \sqrt{y}

$$3\sqrt{2}$$

$$3x\sqrt{2y}$$

$$\sqrt{25(x+2)} = \sqrt{25} \sqrt{x+2}$$
$$5\sqrt{x+2}$$

$$\sqrt{15} \cdot \sqrt{6} = \sqrt{90} = 3\sqrt{10}$$

The diagram illustrates the simplification of the product of two square roots. On the left, $\sqrt{15}$ is factored into $\sqrt{5 \cdot 3}$ and $\sqrt{6}$ is factored into $\sqrt{2 \cdot 3}$. A yellow curved line connects the two '3' factors, indicating they are multiplied together to form a perfect square. This leads to the middle step, $\sqrt{90}$, which is then factored into $\sqrt{9 \cdot 10}$. Finally, $\sqrt{9}$ is simplified to 3, resulting in $3\sqrt{10}$. The '3' in the final result and the '3' in the intermediate $\sqrt{9}$ are highlighted in yellow.

$$3\sqrt[3]{25} \cdot 2\sqrt[3]{5} = 3 \cdot 2 \cdot 5 = 30$$

5 \swarrow 5
5

$$\sqrt[4]{8x^3y^5} \cdot \sqrt[4]{4x^2y^3} = 2xy^2\sqrt[4]{2x}$$

4 \swarrow 2
2 2

2 2
x x x x
y y y y

x
y y y y

Rule #3

$$\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$$

$$\sqrt[3]{\frac{27}{125}} = \frac{\sqrt[3]{27}}{\sqrt[3]{125}} = \frac{3}{5}$$

$$\frac{\sqrt{80}}{\sqrt{5}} = \sqrt{\frac{80}{5}} = \sqrt{16} = 4$$

$$\frac{4\sqrt{5}}{\sqrt{5}}$$



$$\frac{\sqrt[4]{18a^9b^5}}{\sqrt[4]{3b}} = \sqrt[4]{\frac{18a^9b^5}{3b}}$$

$$= \sqrt[4]{6a^9b^4} = a^2b \sqrt[4]{6a}$$

aaaa

aaaa

a

bbbb

$$\frac{1}{\sqrt{2}} \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2}$$

$$\sqrt{\frac{7}{3}} = \frac{\sqrt{7} \sqrt{3}}{\sqrt{3} \sqrt{3}} = \frac{\sqrt{21}}{3}$$

$$\sqrt[3]{\frac{5}{x}} = \frac{\sqrt[3]{5} \sqrt[3]{x} \sqrt[3]{x}}{\sqrt[3]{x} \sqrt[3]{x} \sqrt[3]{x}} = \frac{\sqrt[3]{5x^2}}{x}$$

$\sqrt[3]{x^3}$

$$\frac{\sqrt[5]{3} \sqrt{2} \sqrt{2} \sqrt{2} \sqrt{2}}{\sqrt[5]{2} \sqrt{2} \sqrt{2} \sqrt{2} \sqrt{2}} = \frac{\sqrt[5]{48}}{2}$$